

# Virtual Reality

## 3D Space & Tracking

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# Outline

## Who am I?

## Coordinates in 3D Space

- Position in 3D

- Orientation in 3D

  - Euler angles

  - Axis/angle representation

  - Rotation matrices ( $3 \times 3$ )

  - Quaternions

## Tracking

- Introduction

- Technologies

## VRPN

- What is VRPN

- Simple Example

## Resources

# Who am I?

## PhD from VRlab, EPFL, Switzerland

- ▶ AI for virtual humans, how to make autonomous characters ("NPCs") smarter
- ▶ Lab focused on human character animation, motion capture, interaction in VR
- ▶  $\approx$  20 PhD students, several post-docs, many master students. . .

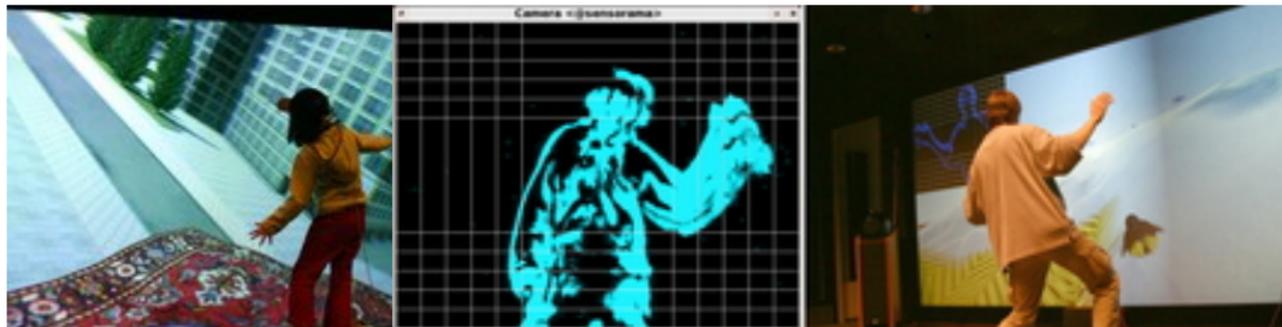


VRlab: <http://vrlab.epfl.ch> IIG: <http://iig.epfl.ch>

# Who am I?

## SensoramaLab, Aalborg University, Denmark

- ▶ Building a new lab focusing on new media, interaction, use in rehabilitation
- ▶ Large projection system, tracking, many interactive demos
- ▶ Teaching bachelor & master students, project supervision.



# Who am I?

## Reviatch SAS

- ▶ Applied research, looking for new technologies useful for our products/customers
- ▶ Tracking, augmented reality, AI, building software & hardware prototypes. . .



<http://www.reviatch.com/>

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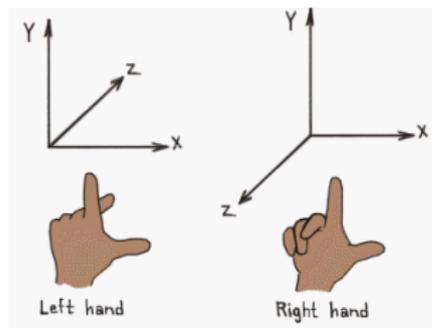
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# 3D Position

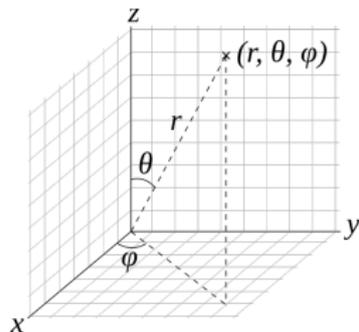


[http://viz.aset.psu.edu/gho/sem\\_notes/3d\\_fundamentals/html/3d\\_coordinates.html](http://viz.aset.psu.edu/gho/sem_notes/3d_fundamentals/html/3d_coordinates.html)

## Cartesian

- ▶ 3 perpendicular axes
- ▶ **Left or right handed!**
- ▶ **Z-up vs Y-up!**
- ▶ Usually same scale on all axes
- ▶ Common units – meters, millimetres, inches, feet. . .

# 3D Position



[http://en.wikipedia.org/wiki/Spherical\\_coordinate\\_system](http://en.wikipedia.org/wiki/Spherical_coordinate_system)

## Spherical

- ▶ Angles  $\theta$ ,  $\phi$ , radius  $r$
- ▶ Conventions! ( $\theta$ ,  $\phi$  could be swapped)
- ▶ GameTrak uses it (see later!)

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# Euler theorem

## Definition

Any two orthonormal three-dimensional coordinate frames can be related by a sequence of rotations (not more than three) about coordinate axes, where no two successive rotations may be about the same axis.

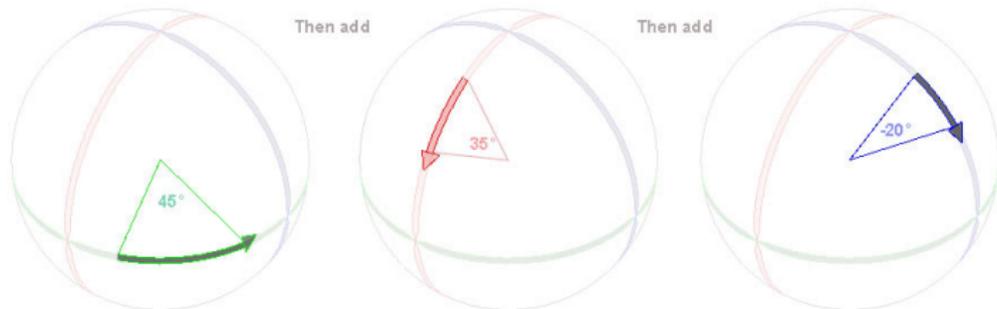
- ▶ Leonard Euler (1707-1783)

# Euler angles

## Euler angles

- ▶ Euler theorem means that we can describe any rotation as a composition of **three basic** rotations around the principal axes.

## Example



[http://www.isner.com/tutorials/quatSpells/quaternion\\_spells\\_14.htm](http://www.isner.com/tutorials/quatSpells/quaternion_spells_14.htm)

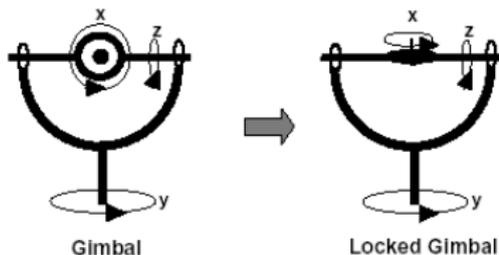
# Euler angles

## Why Euler angles are bad

- ▶ Non-unique way of describing orientation. Rotating in XYZ, ZYX, XZY, ... produces different trajectory for the object. Good for a robot or space ship but not for a human body.
- ▶ Gimbal lock – loss of degree of freedom
- ▶ Conversion to/from a matrix is complex (trigonometry)

## Example

### Gimbal Lock



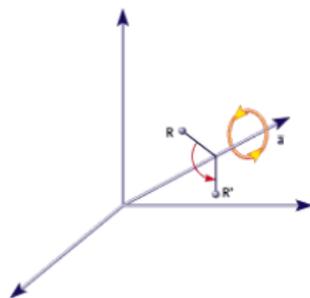
[http://www.cs.duke.edu/courses/fall02/cps124/notes/07\\_rotations/](http://www.cs.duke.edu/courses/fall02/cps124/notes/07_rotations/)

# Axis/angle representation

## Axis/angle representation

- ▶ Axis of rotation (vector) + angle
- ▶ Easy to imagine, no gimbal lock.
- ▶ Very hard to interpolate two rotations :(

## Example



[http://www.cs.duke.edu/courses/fall02/cps124/notes/07\\_rotations/](http://www.cs.duke.edu/courses/fall02/cps124/notes/07_rotations/)

# Rotation matrices

## $3 \times 3$ matrices

- ▶ Non-ambiguous, no gimbal lock, easy to concatenate rotations
- ▶ Very verbose – 9 numbers, compare with 3 for Euler angles or 4 for axis/angle.
- ▶ Non-intuitive
- ▶ Very tricky to interpolate (e.g. turn head from left to right)

## Example

$$\begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \alpha & \sin \alpha \\ 0 & -\sin \alpha & \cos \alpha \end{pmatrix}$$

Rotation around x-axis

$$\begin{pmatrix} \cos \alpha & 0 & -\sin \alpha \\ 0 & 1 & 0 \\ \sin \alpha & 0 & \cos \alpha \end{pmatrix}$$

Rotation around y-axis

$$\begin{pmatrix} \cos \alpha & \sin \alpha & 0 \\ -\sin \alpha & \cos \alpha & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

Rotation around z-axis

# Quaternions

## Description

- ▶ Invented by Hamilton in 1843
- ▶ Deep foundation in algebra
- ▶ Each quaternion has four components:

$$q = [q_0, q_1, q_2, q_3]$$

# Quaternions

## How does it work?

- ▶ Extension to complex numbers
- ▶ 4 components, one is real, 3 are imaginary forming a vector in imaginary  $ijk$  space

## Example

$$q = q_0 + iq_1 + jq_2 + kq_3$$

$$i^2 = j^2 = k^2 = ijk = -1$$

# Quaternions

## Notation

- ▶ Sometimes written as:  $q = \langle s, v \rangle$ , where:

$$s = q_0$$

$$v = [q_1, q_2, q_3]$$

- ▶ Also written as:  $q = [w, q_0, q_1, q_2]$  or  $q = [q_0, q_1, q_2, w]$ , where  $q_i$  are imaginary components and  $w$  is real.
- ▶ **Be very careful which convention is in use if you use some 3rd party library**  $\rightsquigarrow$  hard to find bugs.

# Quaternions

## Unit quaternions

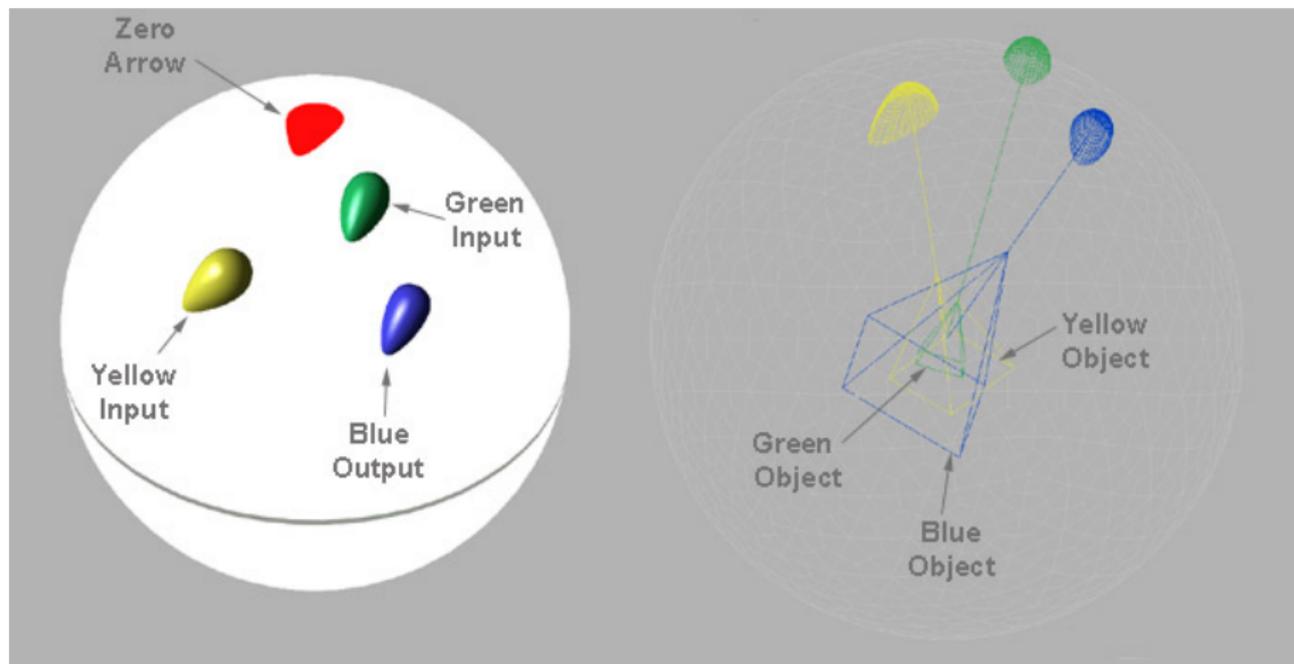
- ▶ Rotations are expressed only using **unit** quaternions:

$$|q| = \sqrt{q_0^2 + q_1^2 + q_2^2 + q_3^2} = 1$$

- ▶ Correspond to a surface of 4D hypersphere of radius 1
- ▶ We have 4D space, but only 3 independent coordinates  $\rightsquigarrow$  representation of a **3D object using 4D coordinates** (similar to spherical coordinates – two angles, radius 1 and the 4th coordinate is a "twist" around this axis).
- ▶ How to visualize that?

# Quaternions

## How quaternions represent orientation/rotations



# Basic properties of quaternions

## Quaternions as rotations

- ▶ Quaternion  $q$  can represent rotation of angle  $\theta$  around an unit axis  $a$ :

$$q = \left[ \cos \frac{\theta}{2}, a_x \sin \frac{\theta}{2}, a_y \sin \frac{\theta}{2}, a_z \sin \frac{\theta}{2} \right]$$

- ▶ Or:

$$q = \left\langle \cos \frac{\theta}{2}, a \sin \frac{\theta}{2} \right\rangle$$

# Basic properties of quaternions

## Axis/angle to quaternion

Axis:  $\vec{v}$

Angle:  $\alpha$

$$q = [w, q_0, q_1, q_2]$$

$$\vec{u} = \frac{\vec{v}}{|\vec{v}|}$$

$$q_i = u_i \sin \frac{\alpha}{2}, i \in [0, 1, 2]$$

$$w = \cos \frac{\alpha}{2}$$

# Basic properties of quaternions

## Quaternion to axis/angle

Quaternion  $q = [w, q_0, q_1, q_2]$

$$\alpha = 2 \arccos w$$

$$v_i = \frac{q_i}{\sqrt{1 - w^2}}, i \in [0, 1, 2]$$

If  $\sqrt{1 - w^2} = 0$  then:

$$v_i = q_i, i \in [0, 1, 2]$$

# Basic properties of quaternions

## Other conversions

- ▶ Left as an exercise for the reader...

See: “Matrix & quaternion FAQ”:

<http://skal.planet-d.net/demo/matrixfaq.htm>

# Basic properties of quaternions

## Angle between two quaternions

- ▶ Dot product of two quaternions:

$$p \cdot q = p_0 q_0 + p_1 q_1 + p_2 q_2 + p_3 q_3 = |p||q| \cos \alpha$$

- ▶ Angle between two quaternions in 4D space is **one half** of the angle needed to rotate the object from one orientation to the other.

# Basic properties of quaternions

## Conjugate and inverse of a quaternion

- ▶ Conjugate:

$$q = [q_0, q_1, q_2, q_3]$$

$$q^* = [q_0, -q_1, -q_2, -q_3]$$

- ▶ Inverse:

$$q^{-1} = \frac{q^*}{|q|^2}$$

# Basic properties of quaternions

## Quaternion multiplication

- ▶ We can multiply quaternions if we expand them into their complex number form:

$$p = p_0 + ip_1 + jp_2 + kp_3$$

$$q = q_0 + iq_1 + jq_2 + kq_3$$

$$pq = (p_0q_0 - p_1q_1 - p_2q_2 - p_3q_3) + i(p_0q_1 + p_1q_0 + p_2q_3 - p_3q_2) \\ + j(p_0q_2 - p_1q_3 + p_2q_0 + p_3q_1) + k(p_0q_3 + p_1q_2 - p_2q_1 + p_3q_0)$$

- ▶ If  $\vec{u} = [p_1, p_2, p_3]$  and  $\vec{v} = [q_1, q_2, q_3]$ :

$$pq = \langle p_0q_0 - \vec{u} \cdot \vec{v}, p_0\vec{v} + q_0\vec{u} + \vec{u} \times \vec{v} \rangle$$

# Basic properties of quaternions

## Quaternion multiplication

- ▶ If quaternions  $p$ ,  $q$  represent rotations, then  $pq$  represents **p rotated by q**
- ▶ Quaternion multiplication is **non-commutative** – i.e. order matters.

# Basic properties of quaternions

## Quaternion multiplication

- ▶ Multiplication of a vector by a quaternion – rotation of a vector:

$$v' = q \cdot v \cdot q^{-1}$$

- ▶ Simpler and faster to calculate than matrix multiplication!

# Summary

## Quaternions

Pros:

- ▶ Compact – only 4 numbers
- ▶ Easy to concatenate, interpolate.
- ▶ Robust – no gimbal lock

Cons:

- ▶ Non-intuitive :(

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# Why tracking?

## Why do we need to track?

- ▶ Interaction – hand, finger
- ▶ Stereoscopy – head tracking
- ▶ Locomotion
- ▶ User activity observation
- ▶ ...

# Terminology

## Degrees of Freedom (DoF)

**Degree of freedom** – one independent parameter describing the movement of an object

## 6 DoF in 3D space

- ▶ Translation  $X, Y, Z$
- ▶ Rotation  $X, Y, Z$

A bit of aside – Euler angles are often called **yaw, pitch, roll**. Which is which axis **depends** – check documentation!



[http://en.wikipedia.org/wiki/Degrees\\_of\\_](http://en.wikipedia.org/wiki/Degrees_of_)

freedom\_







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# Tracking technologies

## Mechanical

- ▶ Linkages + encoders (optical, potentiometres, capacitive. . . )
- ▶ **Pros:** Robust, fast, cheap (usually), excellent accuracy
- ▶ **Cons:** Range
- ▶ **Examples:** Gametrak, FakeSpace BOOM, Phantom, MetaMotion Gypsy



# Tracking technologies

## Magnetic

- ▶ 3 magnetic coils as emitters
- ▶ 3 magnetic coils as receivers (sensors)
- ▶ **Pros:** Robust, fast
- ▶ **Cons:** Complicated math, sensitivity to metal, range
- ▶ **Examples:** Razer Hydra, Flock of Birds, MotionStar, Polhemus. . .



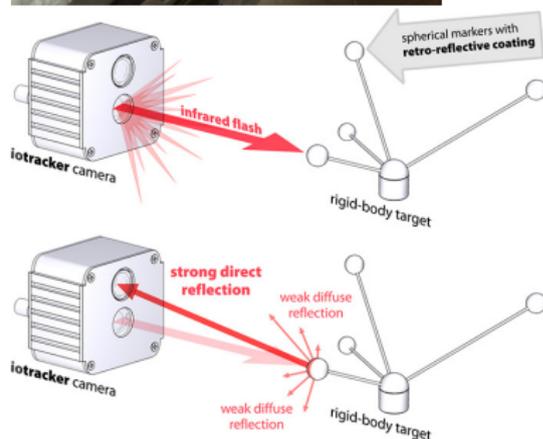
<http://www.sfu.ca/~yma15/iat445/research.html>

<http://souvr SOPHIE.blog.com/page/7/>

# Tracking technologies

## Optical

- ▶ 1+ cameras
- ▶ May or may not use markers
- ▶ **Pros:** Accurate
- ▶ **Cons:** Expensive, difficult for occluded space
- ▶ **Examples:** Vicon, OptiTrack, ARTrack, iotracker, Kinect...



[http://iotracker.com/indexdaed.html?q=optical\\_tracking](http://iotracker.com/indexdaed.html?q=optical_tracking)

# Tracking technologies

## Inertial + hybrid

- ▶ Usually only 3 DoF (orientation)
- ▶ Hybrid systems permit 6 DoF
- ▶ **Pros:** Cheap, self-contained
- ▶ **Cons:** Limited DoF, mocap
- ▶ **Examples:** Wiimote, PS Move, XSens...



<http://www.xsens.com/products/xsens-mvn/>



# Low cost tracking

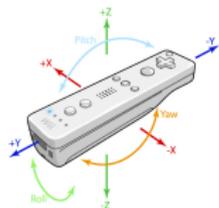
## Low cost is relative

- ▶ In "pro" field anything  $\leq 10000\text{€}$  is considered low cost. . .
- ▶ "Enthusiast" low cost  $\leq 500\text{€}$

## Devices (not exhaustive list)

- ▶ Wiimote
- ▶ PS Move
- ▶ Kinect (Asus Xtion, etc)
- ▶ GameTrak
- ▶ Leap Motion
- ▶ Razer Hydra (STEM)
- ▶ Novint Falcon
- ▶ Freetrack
- ▶ TrackIR
- ▶ Webcam (ARToolkit, . . . )

# Low cost tracking



Wiimote



PS Move



Kinect



GameTrak



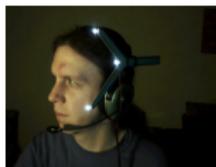
Leap Motion



Razer  
Hydra



Novint  
Falcon



Freetrack



Track IR



Webcam

# Low cost tracking

## IMUs

- ▶ Useful for head tracking (3DoF)
- ▶ Combine with Kinect or GameTrak for full 6DoF!
- ▶ Usually requires an Arduino or something similar (electronics)
- ▶ Ready-made ones are expensive (e.g. Inertia Cube  $\approx$  600€!)

## Where to get one

- ▶ Just use Wiimote (simplest, ugly)
- ▶ US: SparkFun (expensive, but support)
- ▶ China: DealXtreme, AliExpress (cheap, easy to get ripped off!)
- ▶ Build one! (Can you solder 3x3mm lead-less 24pin chip?)

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# What is VRPN?

## Virtual Reality Peripheral Network

- ▶ <http://www.cs.unc.edu/Research/vrpn/>
- ▶ Originally research project, University of Northern Carolina Chapel Hill, maintainer Russell M. Taylor II
- ▶ Industry standard, almost every tracker, motion capture system and VR device supports it
- ▶ Open source, portable, free to use

# What is VRPN?

## Virtual Reality Peripheral Network

- ▶ Low latency/overhead
- ▶ Simple to use
- ▶ Network transparent
- ▶ Device abstraction & factoring
- ▶ Device sharing between multiple applications
- ▶ Many devices supported natively

# Device abstraction

## Types of devices

Analog	float value $\in \langle -1, 1 \rangle$ , e.g. joystick axis
Button	Abstract button on/off
Dial	Incremental rotation, e.g. Griffin Powermate jog wheel
ForceDevice	Force feedback devices, e.g. Novint Falcon
Sound	Sound generators
Text	Allows passing text messages to/from the device
Tracker	Abstract 6DoF tracker class

# Device abstraction

## Device factorization

- ▶ Every device can be decomposed into abstract devices
- ▶ Applications only need to support the abstract device types, never specific hardware!

## Example

Razer Hydra	1 6DoF tracker (2 sensors), 14 buttons, 2 analogs (triggers)
Wiimote	11 buttons, 3 analogs (6 if Motion+ installed)
Kinect	6DoF tracker with 15 sensors, however, some return only 3DoF data (position)

# VRPN

## Server

- ▶ Native, see `vrpn.cfg` – all supported devices are documented there
- ▶ 3rd party – e.g. OptiTrack or other vendors provide VRPN compatible servers for their hw.
- ▶ One server can handle multiple devices!
- ▶ **Device ID:** `device@host:port`, e.g.  
`Hydra0@192.168.1.1:5000`

## Client(s)

- ▶ Receive data from the server over TCP/IP
- ▶ Typically some sort of 3D/VR application
- ▶ Make sure firewall isn't blocking it (both TCP and UDP needed!)

# VRPN – Coordinate systems

## Device to Sensor $M_{d2s}$

Fixed offset between the "active" part of the tracked object & the marker (we measure it).

## Sensor to Tracker $M_{s2t}$

Position/orientation of the sensor relative to the tracker origin/base (tracker reports this).

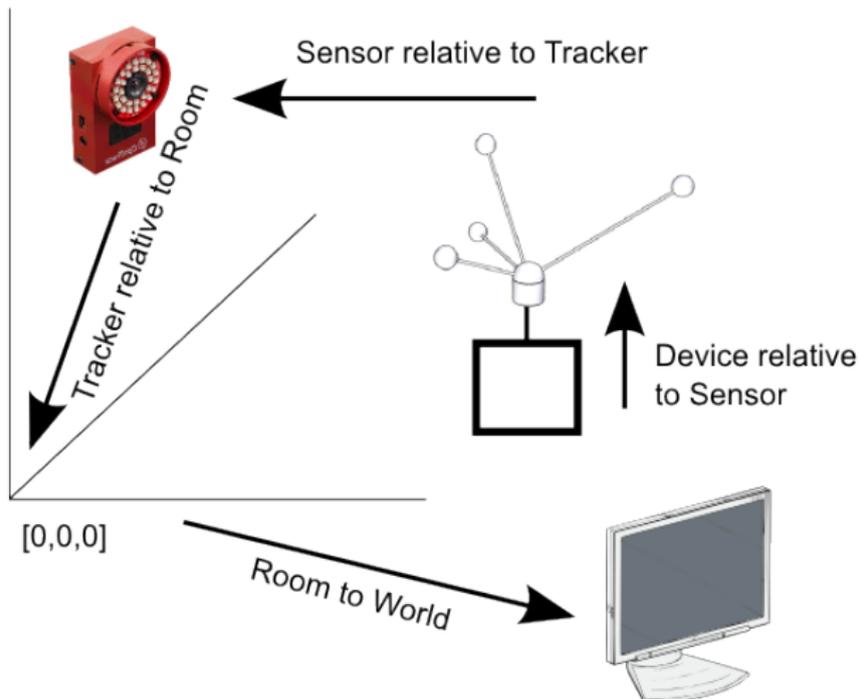
## Tracker to room $M_{t2r}$

Positions the tracker in the physical space – the origin of the tracker doesn't always correspond to the origin of the room!

## Room to world $M_{room2world}$

Adapts the 3D rendering coordinates to match the physical space (not always required).

# VRPN – Coordinate systems



## VRPN – Coordinate systems

### Moving an object in the 3D world

Object transformation matrix:

$$M_{sensor} = (M_{s2t} \times M_{d2s})$$

$$M_{world} = M_{room2world} \times M_{t2r} \times M_{sensor} \times M_{t2r}^{-1} \times M_{room2world}^{-1}$$

$$p'_{world} = M_{world} \times p_{world}$$

### Why handling position & orientation separately?

- ▶ If you don't it would translate in a rotated coordinate space or rotate around a translated origin.
- ▶ Likely not what you want!

# VRPN – Coordinate systems

## Determining the matrices

- ▶  $M_{room2world}$ ,  $M_{t2r}$ ,  $M_{d2s}$  are **constant!**
- ▶  $M_{d2s}$  can be measured (calipers, ruler, etc.)
- ▶  $M_{room2world}$  is arbitrary, depends on the app (can be identity!)
- ▶  $M_{t2r}$  can be determined by calibration, typically orientation + scale of the tracker relative to the room.

# VRPN – Coordinate systems

## Simple calibration procedure

1. Move sensor one meter to the front, then to the right from the same spot (desired room origin).
2. Record the 3 points  $p_1, p_2, p_3$  reported by the tracker.
3. Calculate vectors:  $\vec{v}_x = p_2 - p_1$ ,  $\vec{v}_y = p_3 - p_1$ ,  $\vec{v}_z = \vec{v}_x \times \vec{v}_y$
4. Normalize:  $\vec{n}_x = \frac{\vec{v}_x}{|\vec{v}_x|}$ ,  $\vec{n}_y = \frac{\vec{v}_y}{|\vec{v}_y|}$ ,  $\vec{n}_z = \frac{\vec{v}_z}{|\vec{v}_z|}$
5. Assemble the matrix:  $M_{t2r}^{-1} = \begin{pmatrix} n_x[0] & n_y[0] & n_z[0] & 0 \\ n_x[1] & n_y[1] & n_z[1] & 0 \\ n_x[2] & n_y[2] & n_z[2] & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$
6. The vectors are orthogonal, so we can transpose instead of inverting to obtain  $M_{t2r}$ :  $M_{t2r} = (M_{t2r}^{-1})^T$

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# Simple example

## VRPN tutorial

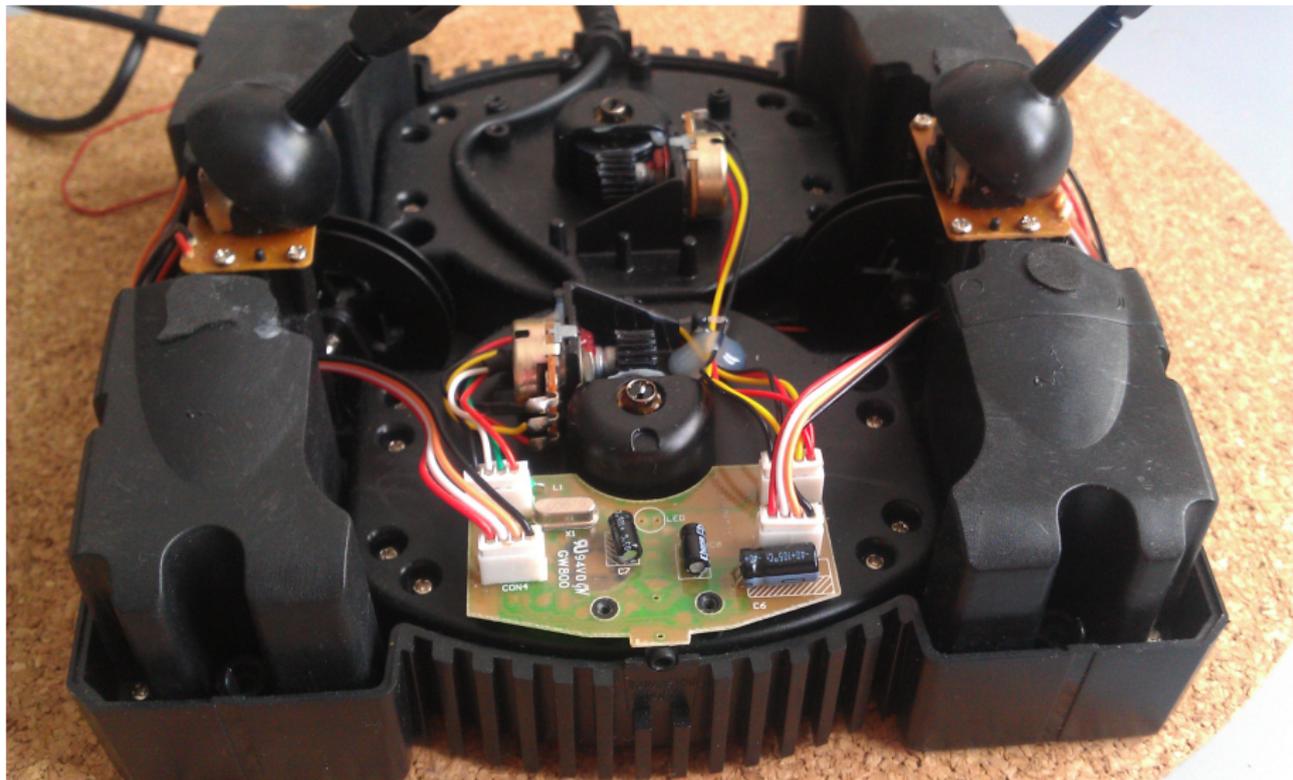
`http://www.vrgeeks.org/vrpn/tutorial---use-vrpn`

# Resources

## Few useful links

- ▶ **Quaternion FAQ** [http://www.j3d.org/matrix\\_faq/matrfaq\\_latest.html](http://www.j3d.org/matrix_faq/matrfaq_latest.html)
- ▶ **VR Geeks** <http://www.vrgeeks.org/>
- ▶ **VRPN** <http://www.cs.unc.edu/Research/vrpn/>
- ▶ **GlovePie** <http://glovepie.org/glovepie.php>
- ▶ **FreeTrack** <http://www.free-track.net/english/>
- ▶ **Wiiuse** <http://public.vrac.iastate.edu/~rpavlik/doxygen/wiiuse-fork/>
- ▶ **GameTrak hacking** <http://janoc.rd-h.com/archives/129>
- ▶ **FAAST** <http://projects.ict.usc.edu/mxr/faast/>
- ▶ **Free version of Unity 3D + VRPN requires hacks**  
<https://github.com/TermWay/UniVRPNity>
- ▶ **MiddleVR** <http://www.imin-vr.com/middlevr-for-unity/>

# GameTrak



# GameTrak

